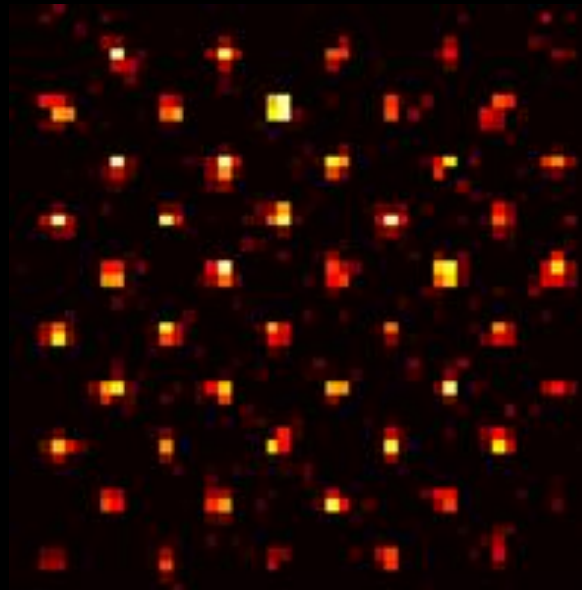


Quantum simulation of spin Hamiltonians in arrays of single Rydberg atoms: recent results, work in progress, and new tools

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*Laboratoire Charles Fabry,
CNRS, Institut d'Optique, Palaiseau, France*



The Rydberg team in Palaiseau

**Antoine
Browaeys**



**Thierry
Lahaye**



**Vincent
Lienhard**



**Sylvain
de Léséleuc**



**Daniel
Barredo**



**Florence
Nogrette**



Former members:

A. Vernier, L. Béguin, H. Labuhn, S. Ravets

Group website: <https://atom-tweezers-io.org/>

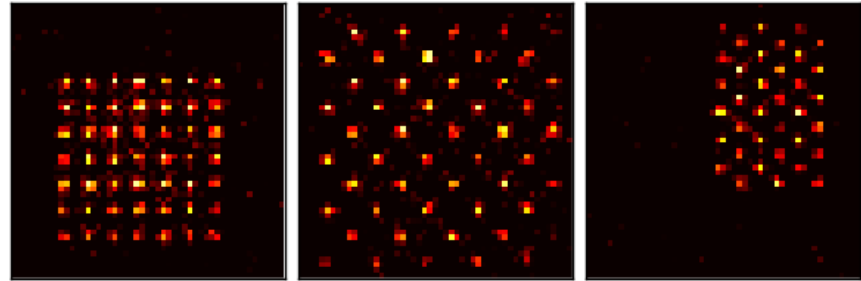
Funding:



Our experimental platform

- **Arrays of single atoms with arbitrary geometries**

Spacing: a few microns



- **Strong interactions via Rydberg excitation**

$$U / h \sim 1\text{-}10 \text{ MHz for } R \sim 5\text{-}10 \text{ }\mu\text{m}$$

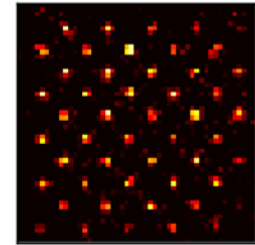
Implement spin models

Ising (vdW interactions), XY (resonant dipole-dipole interaction),...

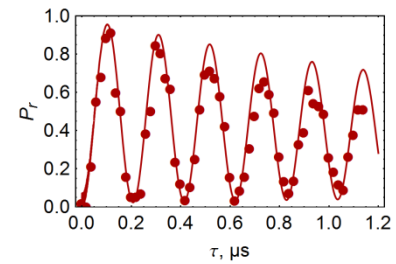
(...but also quantum gates!)

Outline

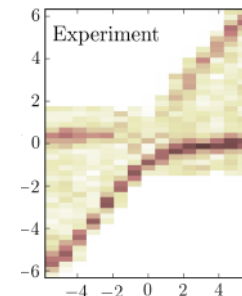
1. Setup and recent results



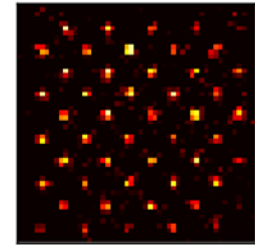
2. Understanding imperfections



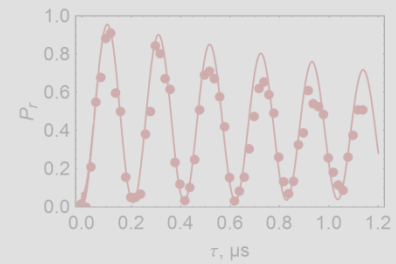
3. Some new tools



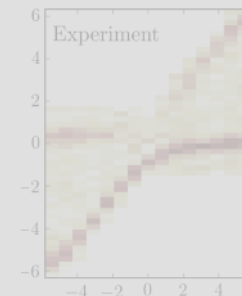
1. Setup and recent results



2. Understanding imperfections

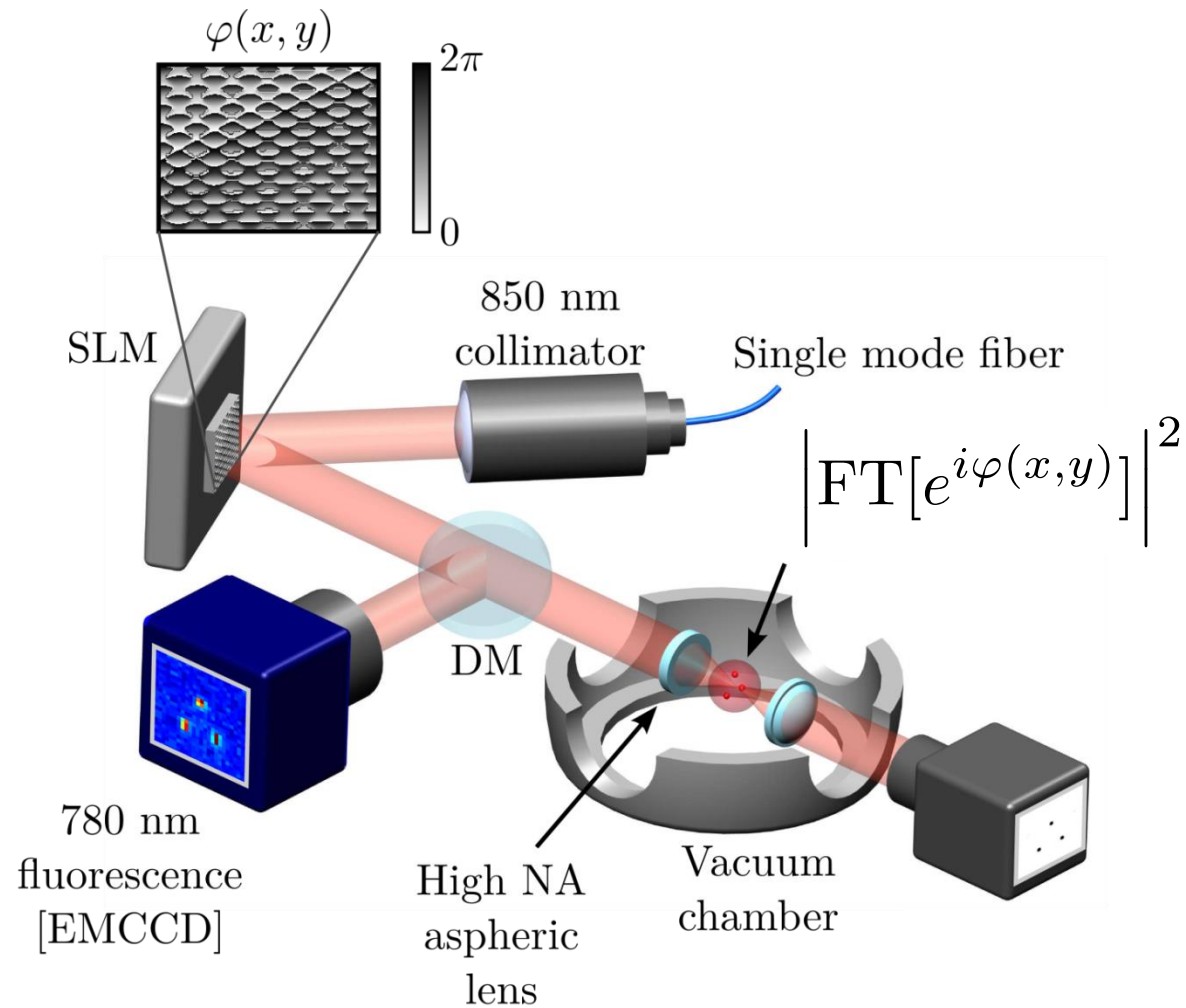


3. Some new tools



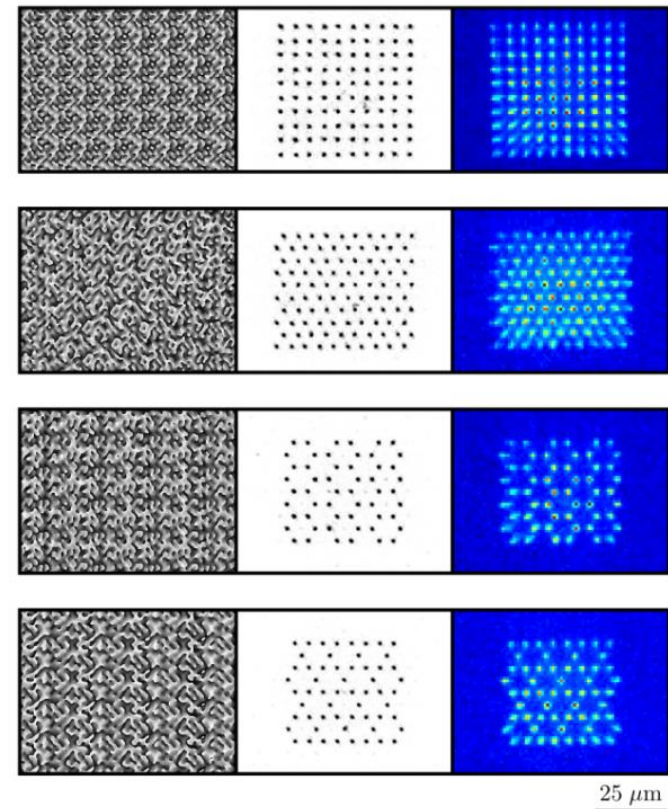
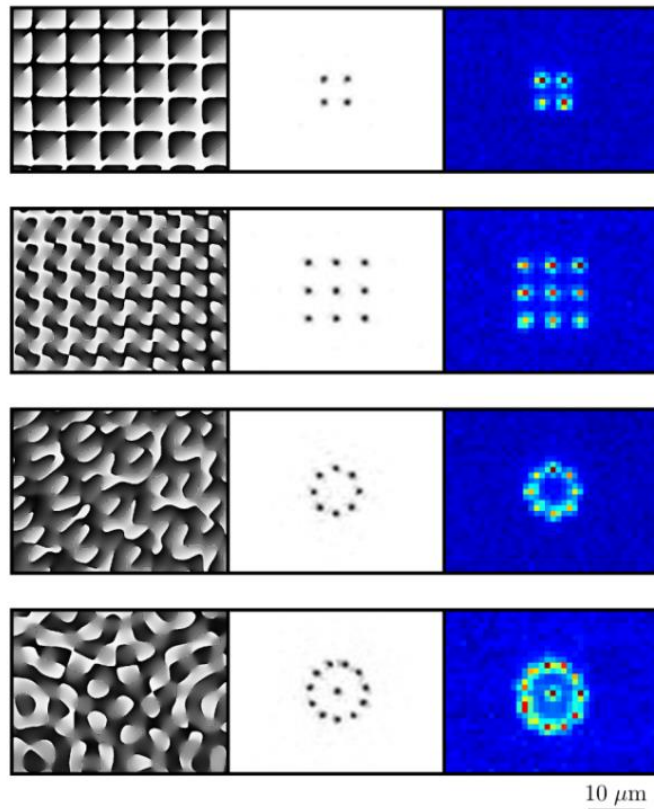
2D arrays of single atoms

Arrays of microtraps with an SLM



+ 8 independent electrodes under vacuum to control electric field

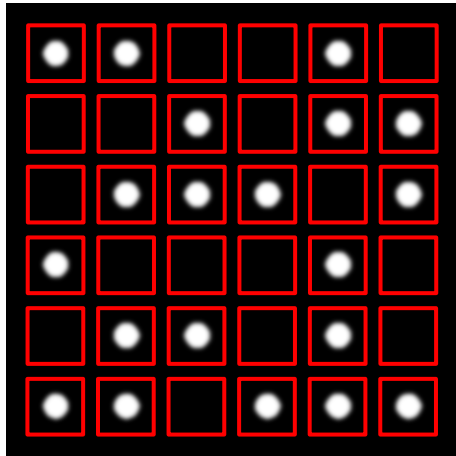
A gallery of arrays



- Distance between neighboring traps down to 3 μm
- Highly uniform trap depths
- Easily reconfigurable

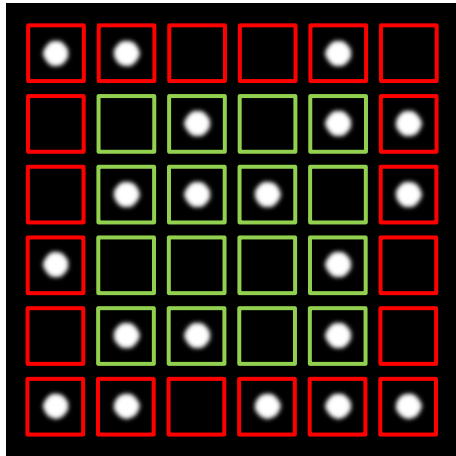
Active sorting of the atoms in the arrays

**Initial atom distribution
(stochastically filled)**



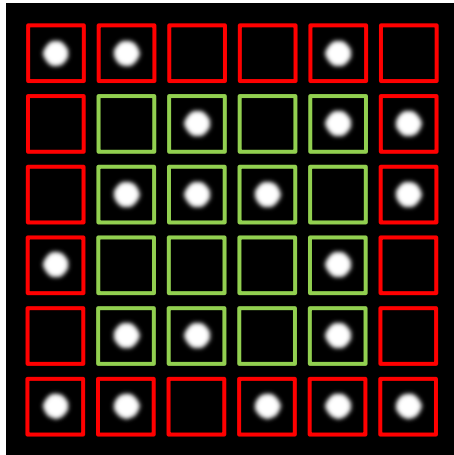
Active sorting of the atoms in the arrays

Initial atom distribution
(stochastically filled)

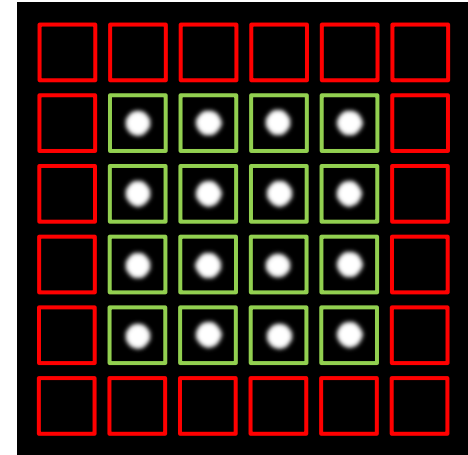


Active sorting of the atoms in the arrays

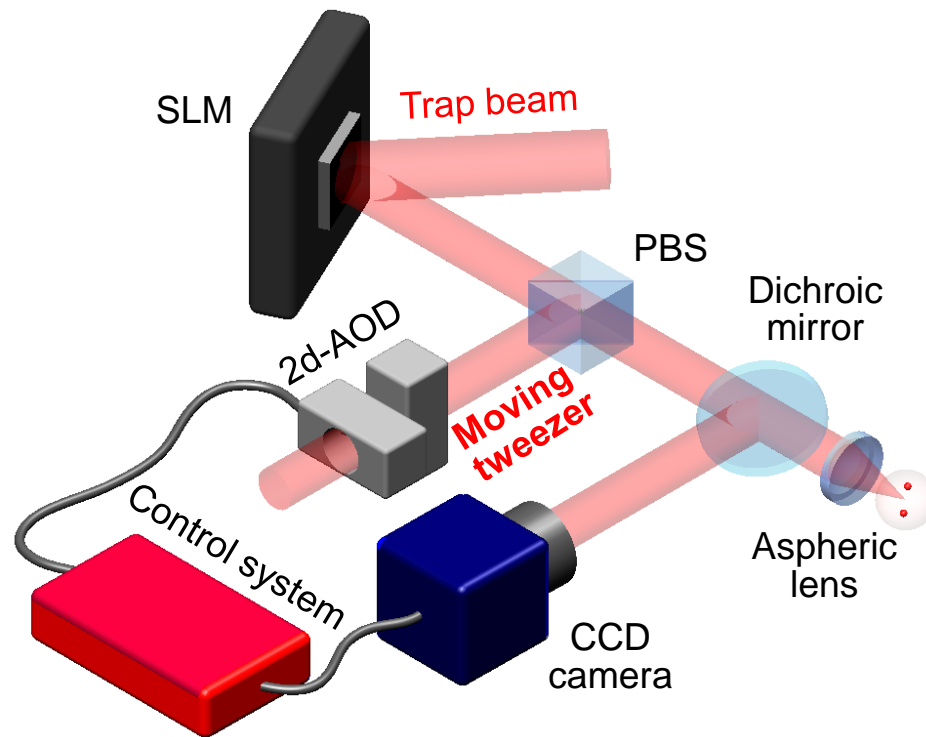
**Initial atom distribution
(stochastically filled)**



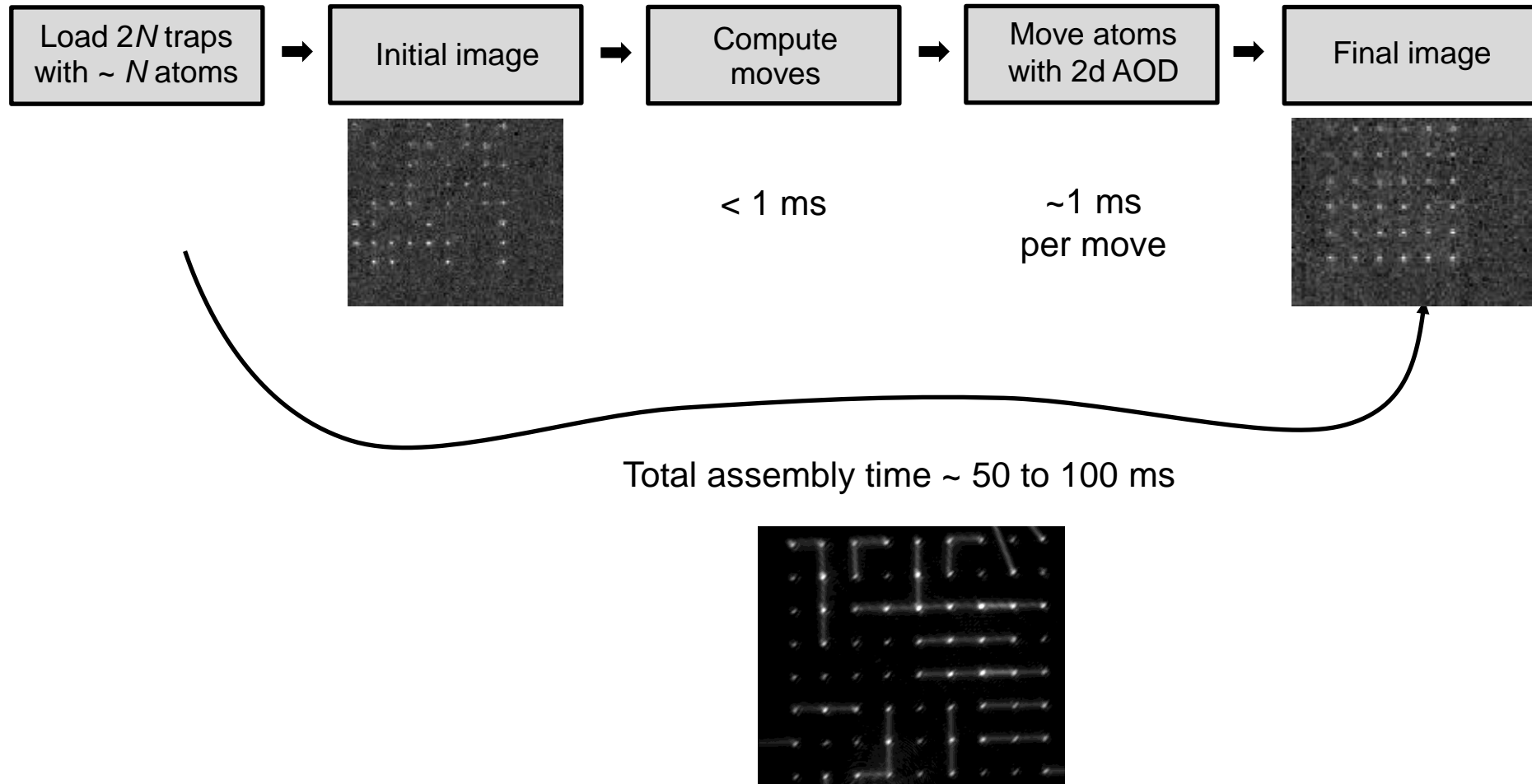
**Target atom distribution
(ordered array)**



How? Moving optical tweezers!

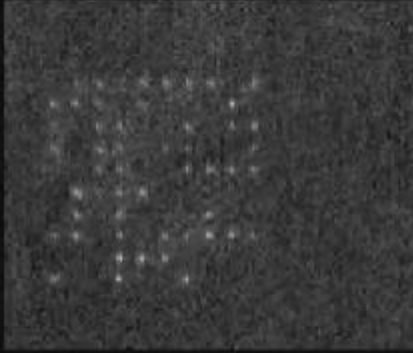


Assembly sequence for a target of N traps

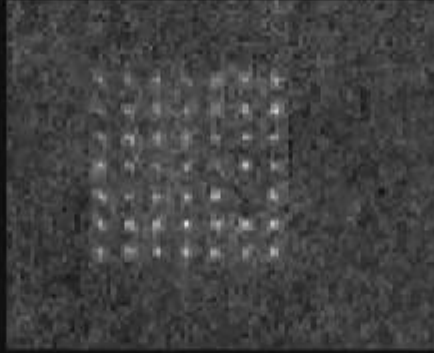


Assembly of a 7x7 square array

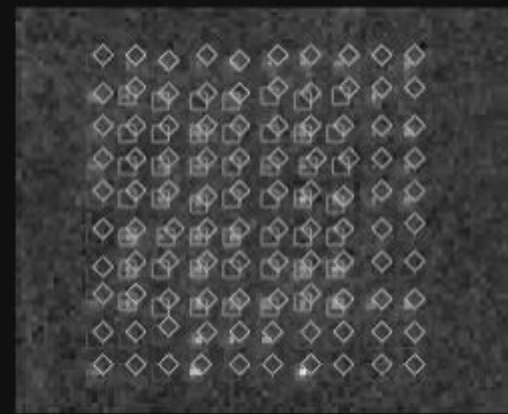
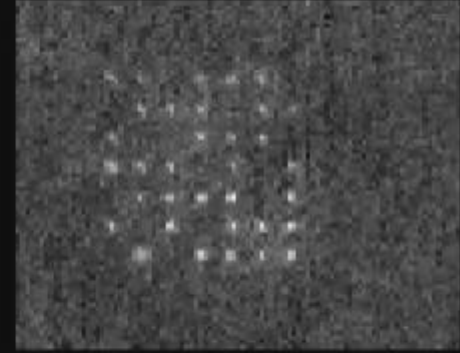
Before sorting



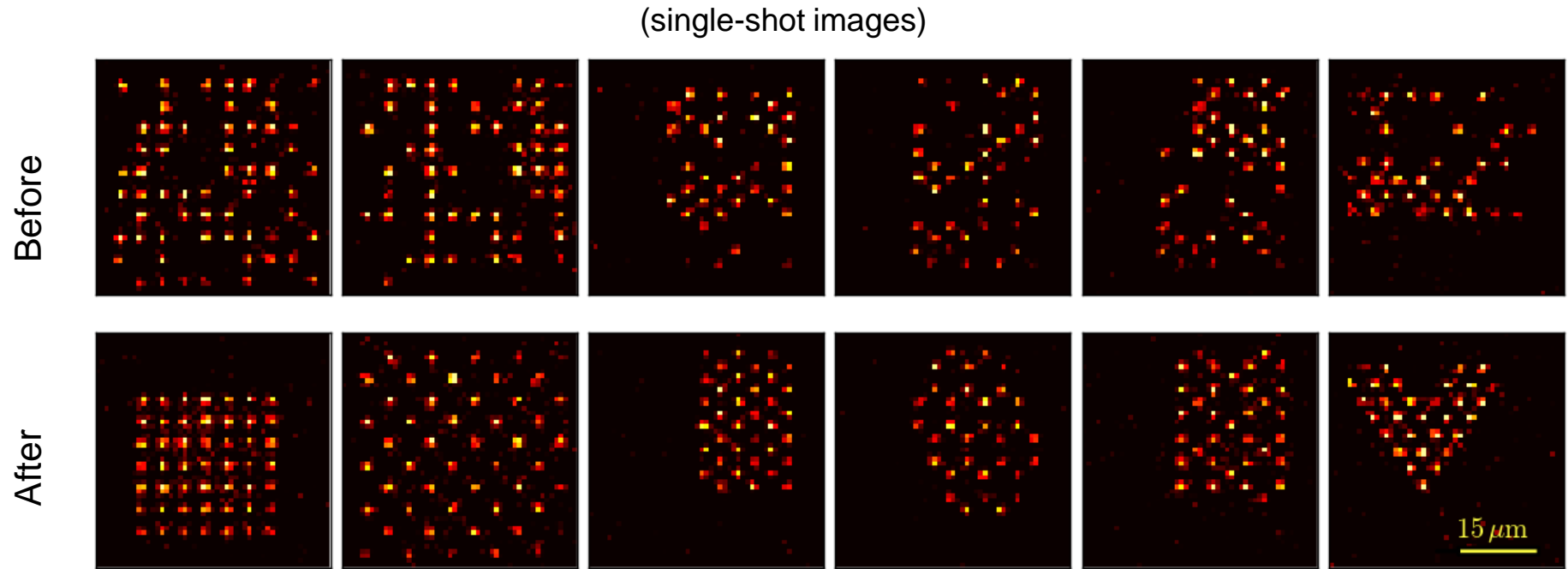
After sorting



After Rydberg excitation



Gallery of arrays



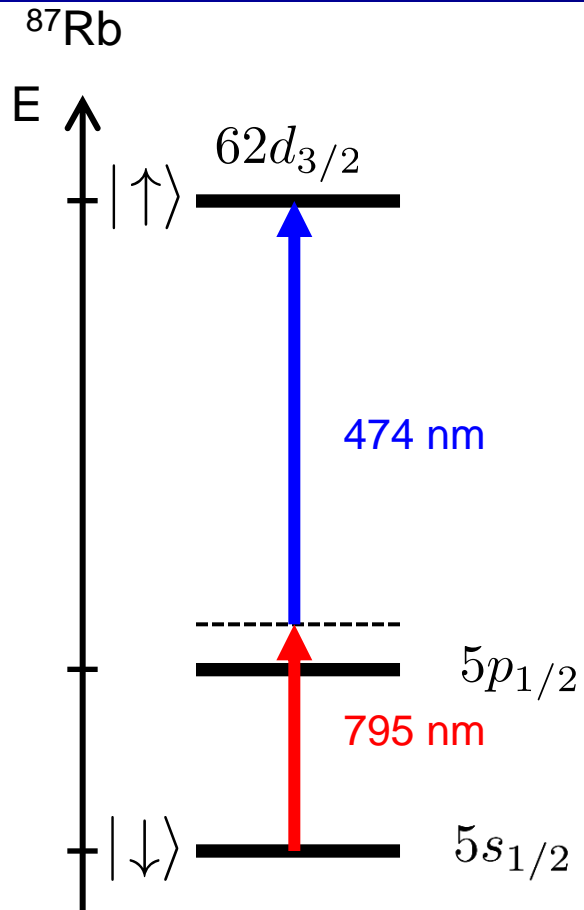
- Fully loaded arrays up to 50 atoms
- 98% filling fraction at $\sim 1/\text{s}$ repetition rate
- 100% filling every $\sim 2\text{-}5$ sec

Barredo, de Léséleuc, *et al.*, Science **354**, 1021 (2016)

Related work at Harvard in 1D: Science **354**, 1024 (2016)

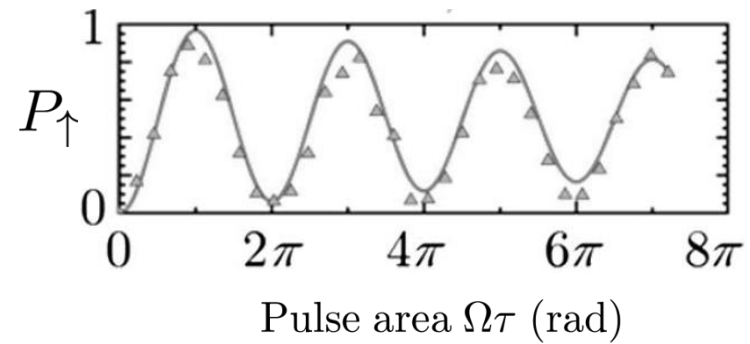
Rydberg atoms & their interactions

Coherent manipulation of Rydberg states

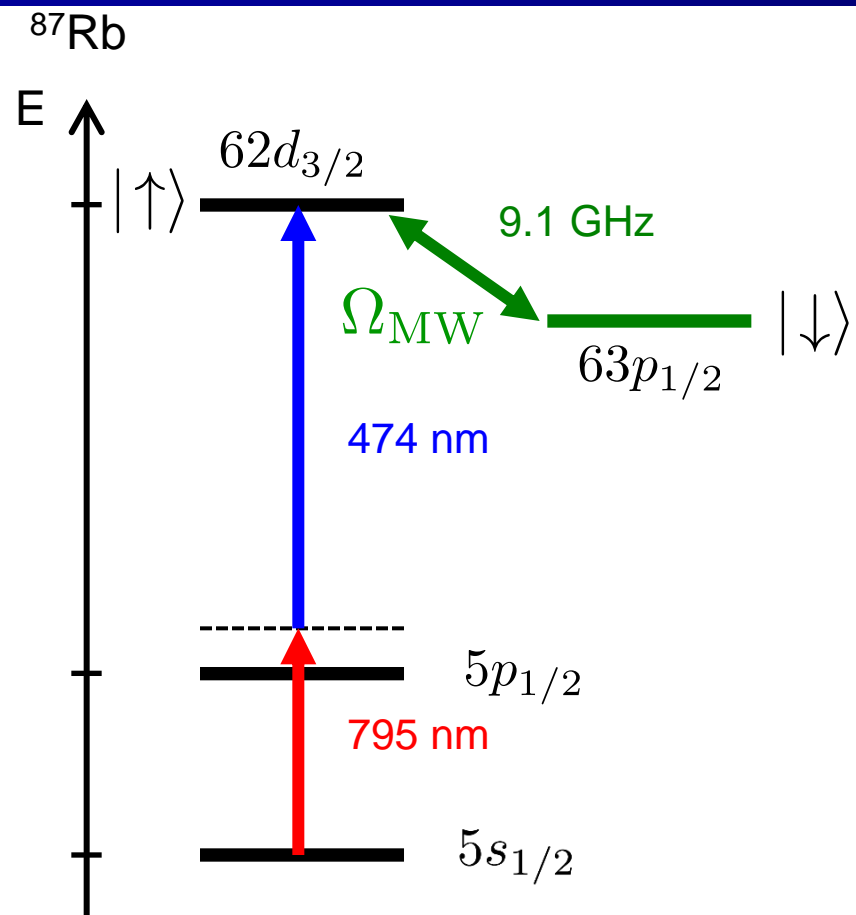


Single atom \Rightarrow repeat 100 times

Optical excitation $\Omega/(2\pi) \sim 1 \text{ MHz}$

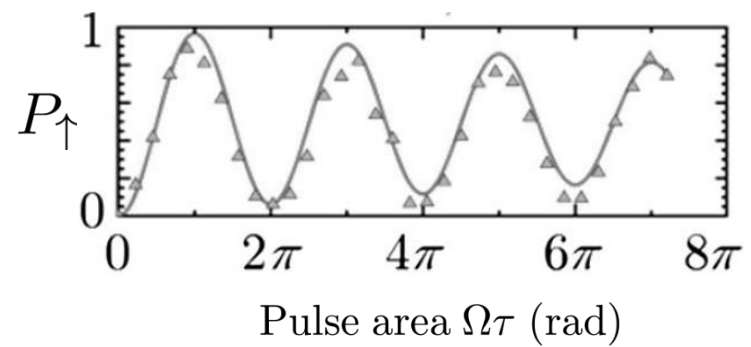


Coherent manipulation of Rydberg states

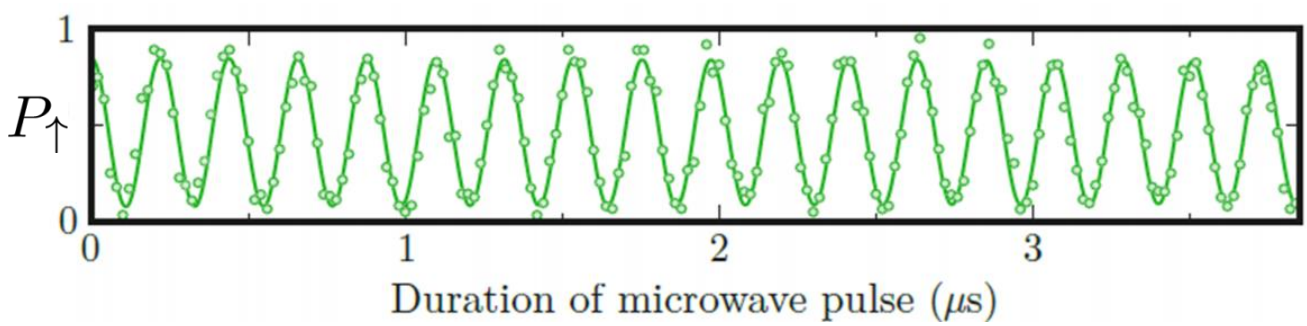


Single atom \Rightarrow repeat 100 times

Optical excitation $\Omega/(2\pi) \sim 1\text{ MHz}$

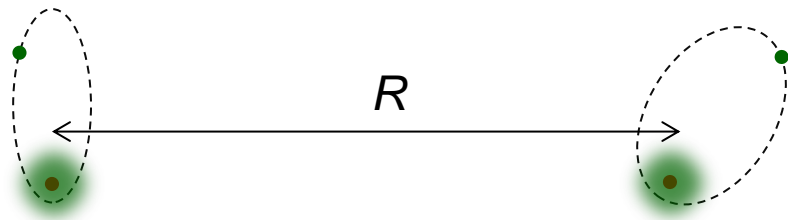


Microwave transfer



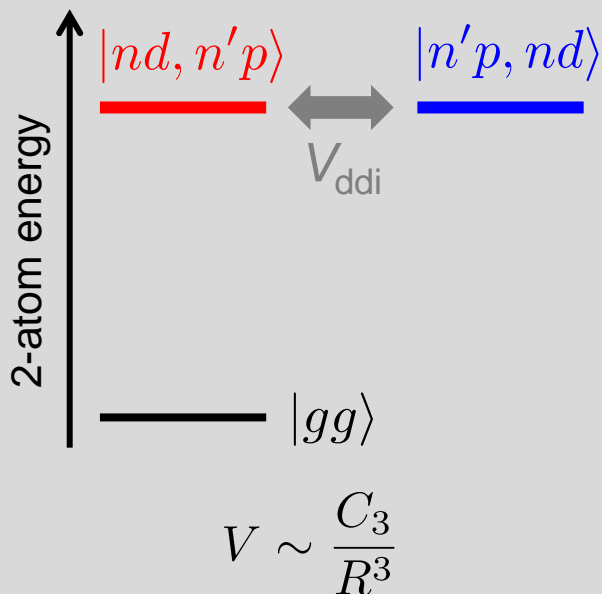
D. Barredo *et al.*,
PRL **114**, 113002 (2015)

Interactions between Rydberg atoms



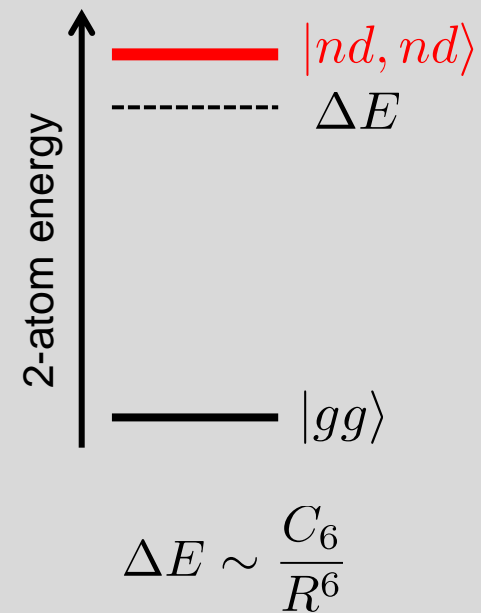
$$\hat{V}_{\text{ddi}} = \frac{1}{4\pi\epsilon_0} \frac{\hat{\mathbf{d}}_1 \cdot \hat{\mathbf{d}}_2 - 3(\hat{\mathbf{d}}_1 \cdot \hat{\mathbf{n}})(\hat{\mathbf{d}}_2 \cdot \hat{\mathbf{n}})}{R^3}$$

Resonant interaction



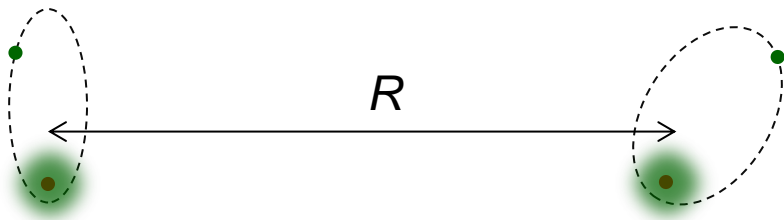
XY interaction (flip-flop)

van der Waals



Ising-like interaction

Interactions between two Rydberg atoms in the lab



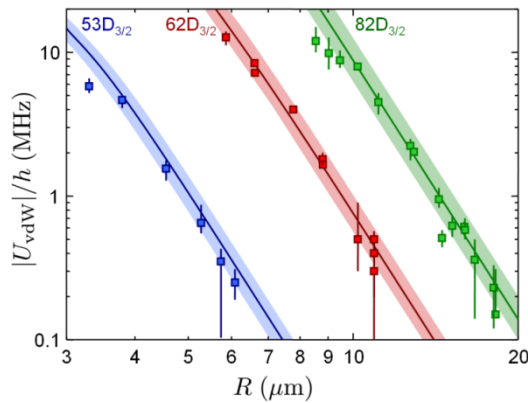
$$\hat{V}_{\text{ddi}} = \frac{1}{4\pi\epsilon_0} \frac{\hat{\mathbf{d}}_1 \cdot \hat{\mathbf{d}}_2 - 3(\hat{\mathbf{d}}_1 \cdot \hat{\mathbf{n}})(\hat{\mathbf{d}}_2 \cdot \hat{\mathbf{n}})}{R^3}$$

van der Waals

Förster resonance

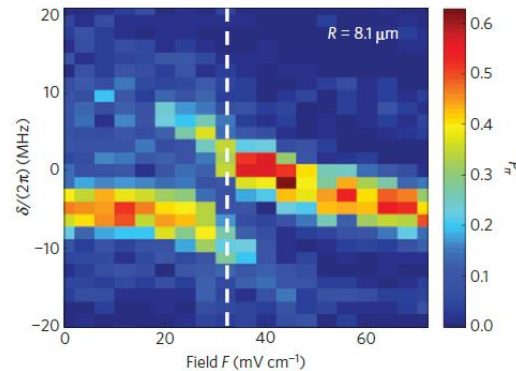
Resonant dipole-dipole interaction

$$U \sim 1/R^6$$



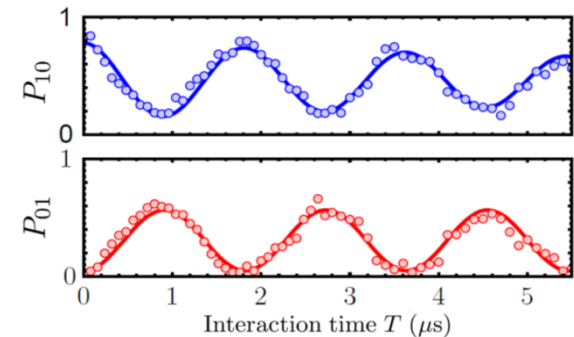
Béguin *et al.*, PRL 2013

$$U \sim 1/R^3$$



Ravets *et al.*, Nature Phys. 2014

$$U \sim 1/R^3$$



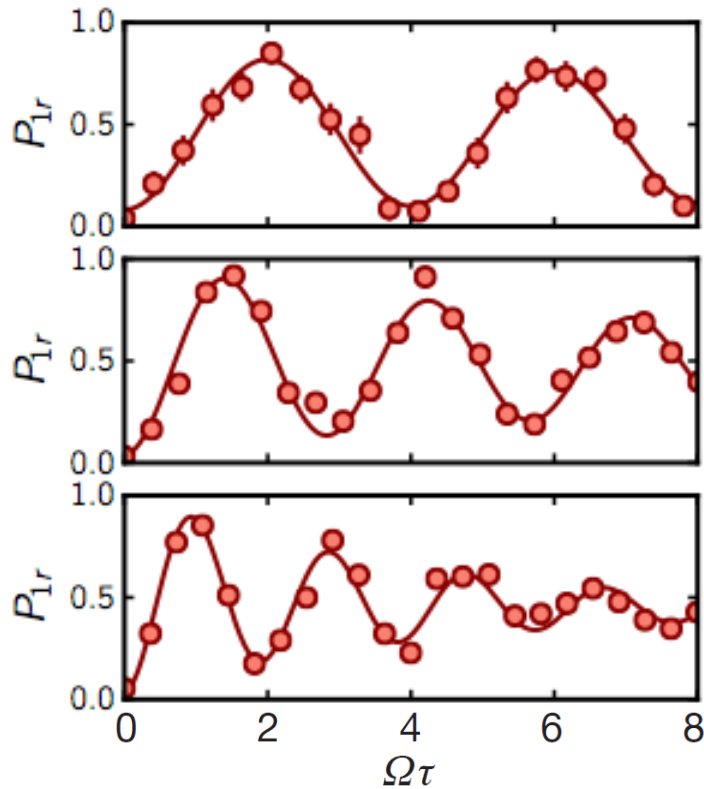
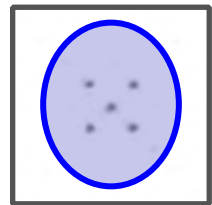
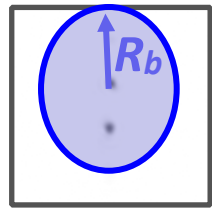
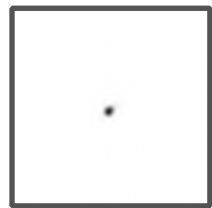
Barredo *et al.*, PRL 2015

Review: A. Browaeys *et al.*, J. Phys. B **49**, 152001 (2016)

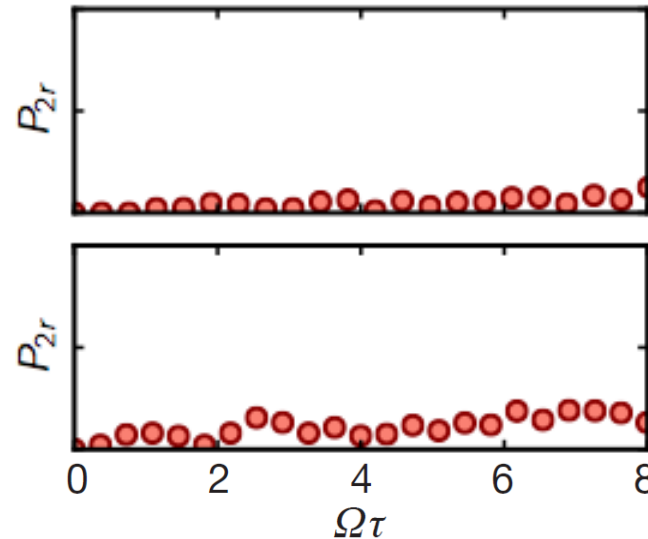
Rydberg blockade and Ising-like spin Hamiltonians

Collective excitation & Rydberg blockade

1 Rydberg excitation

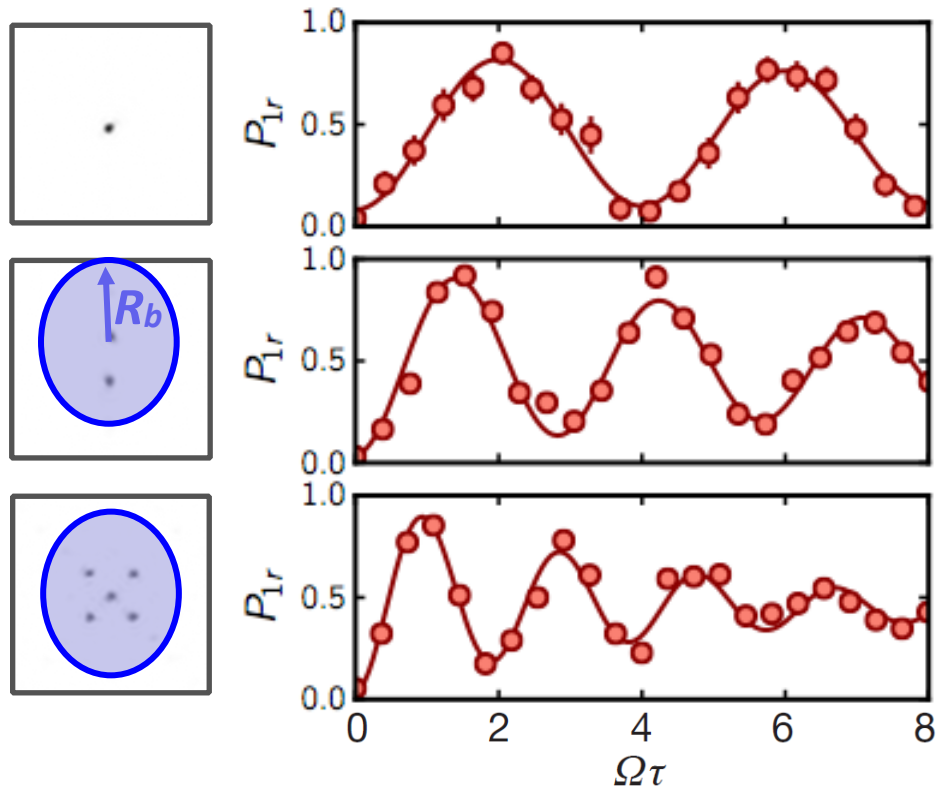


2 Rydberg excitations

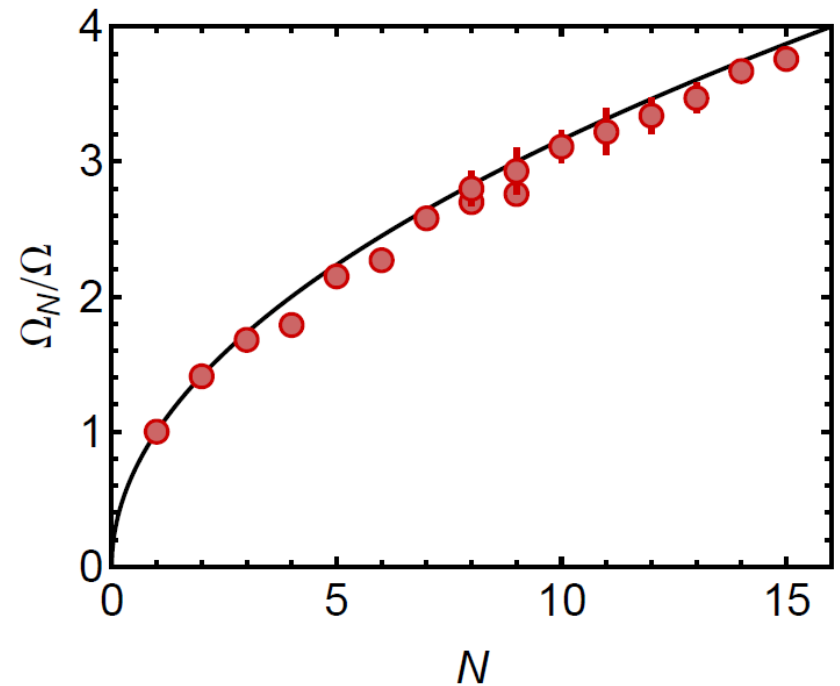


Collective excitation & Rydberg blockade

1 Rydberg excitation



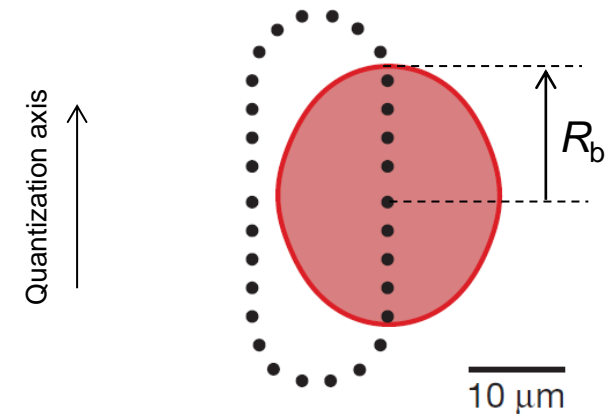
Collective enhancement



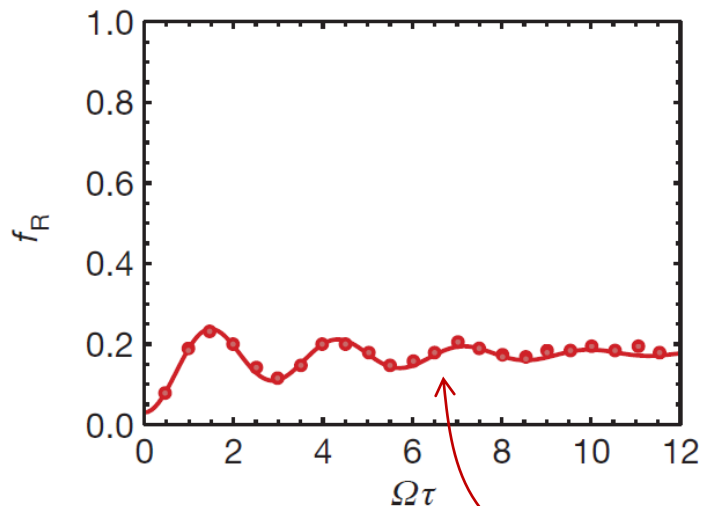
Quench of Ising-like spin Hamiltonians

1D chain with periodic boundary conditions
20 atoms

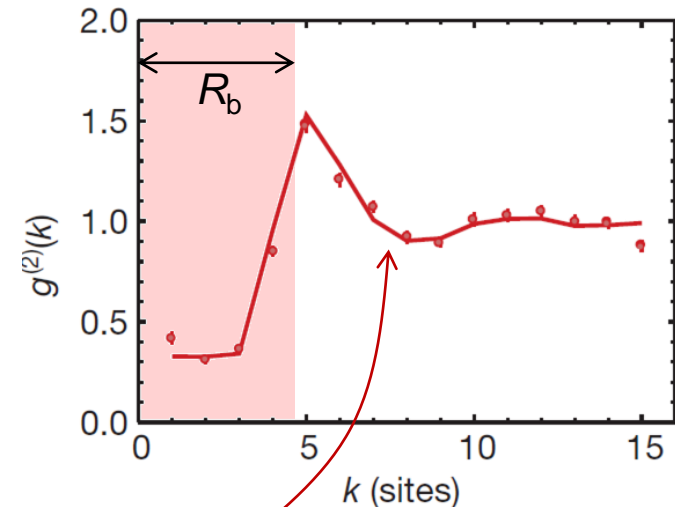
$$H = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i + \sum_{i<j} V_{ij} n^i n^j$$



Magnetization

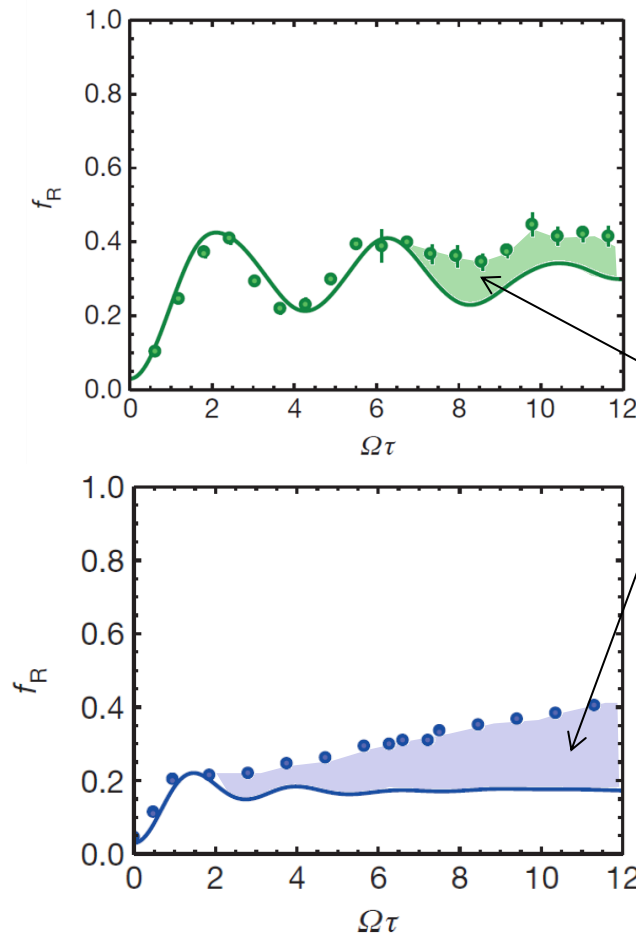
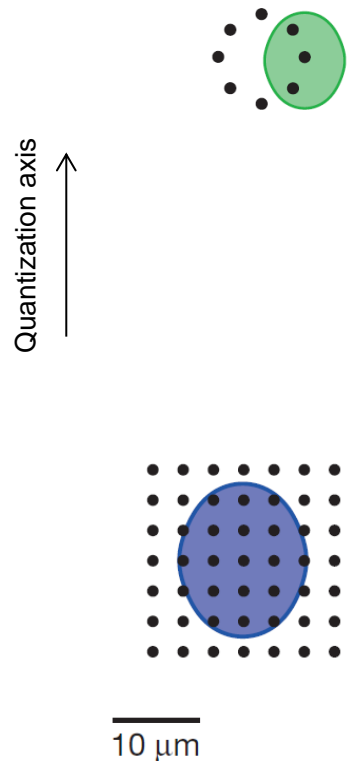


Spin-spin correlation function



Spin $\frac{1}{2}$ model, no adjustable parameter
(calculations by Tommaso Macrì)

Quench of Ising-like spin Hamiltonians



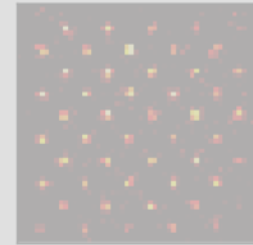
Stronger anisotropy

Excess of Rydberg atoms at long times as compared to prediction of spin $\frac{1}{2}$ model

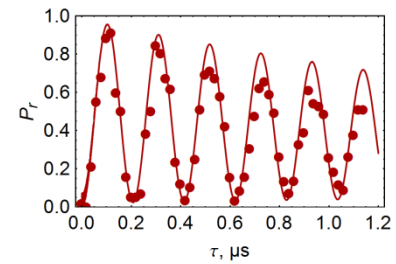
Effect of multilevel structure of $D_{3/2}$ Rydberg states?

Outline

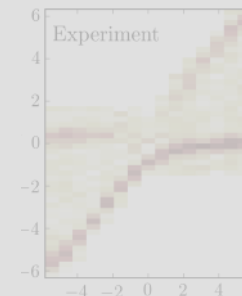
1. Setup and recent results



2. Understanding imperfections



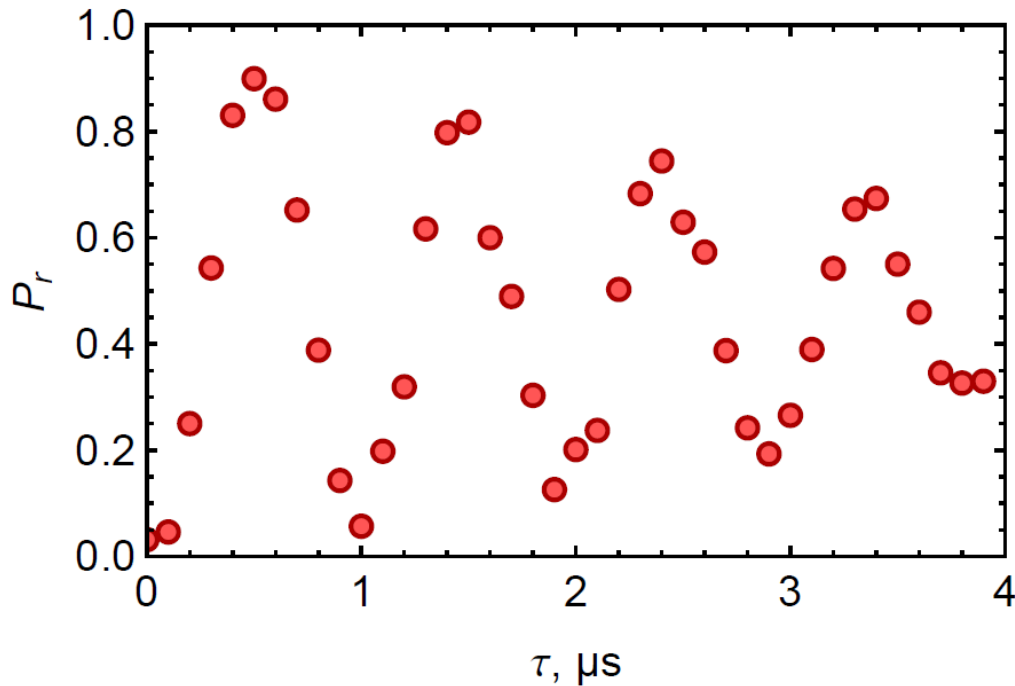
3. Some new tools



Imperfections at the single-particle level

Understanding the damping of Rabi oscillations $|g\rangle \leftrightarrow |r\rangle$

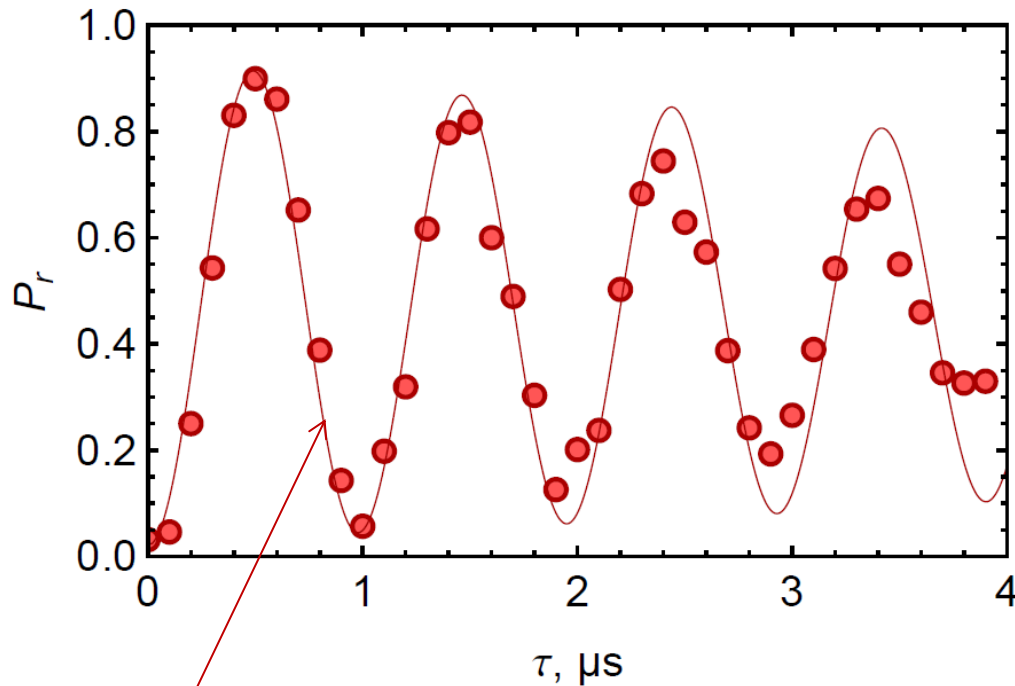
Typical Rabi oscillation to $61D_{3/2}$ for a single atom:



1/e damping time $\sim 5 \mu\text{s}$. Where does this come from?

Understanding the damping of Rabi oscillations $|g\rangle \leftrightarrow |r\rangle$

Typical Rabi oscillation to $61D_{3/2}$ for a single atom:



Model including a, b, c, d. No adjustable parameter.

Combination of several small effects:

- a. Doppler effect
- b. Spontaneous emission via $5P_{1/2}$ state
- c. Laser phase noise
- d. Imperfection in optical pumping and in detection

More details in the “decoherence” session...

***Imperfect blockade for nD states
due to anisotropic vdW interactions***

Breakdown of Rydberg blockade

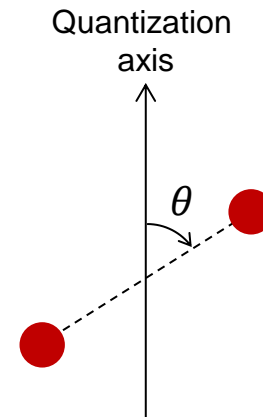
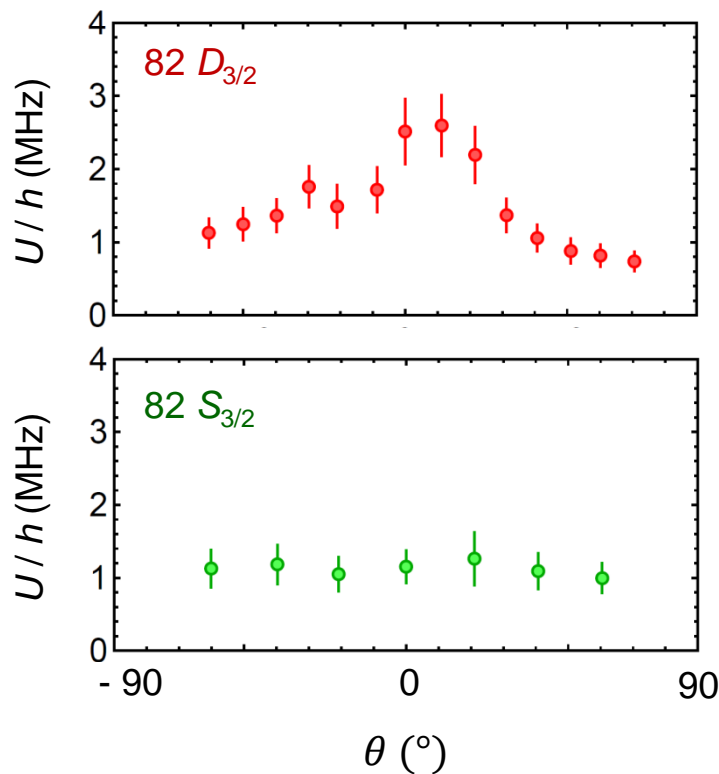
Rydberg atoms have *many* levels...

...which can lead
to a breakdown
of the blockade:

- ***Zeeman degeneracies***
T. G. Walker and M. Saffman, Phys. Rev. A **77**, 032723 (2008).
- ***'Three-body' interactions close to Förster resonances***
T. Pohl and P.R. Berman, Phys. Rev. Lett. **102**, 013004 (2009).
- ***Molecular resonances***
A. Derevianko *et al.*, Phys. Rev. A **92**, 063419 (2015).

Understanding the imperfect blockade for D states

- $nD_{3/2}$ states: 4 Zeeman sublevels
- For an atom pair not aligned with quantization axis, vdW interaction is a 16 x 16 matrix
- Simplest approach: Anisotropic, effective C_6 coefficient

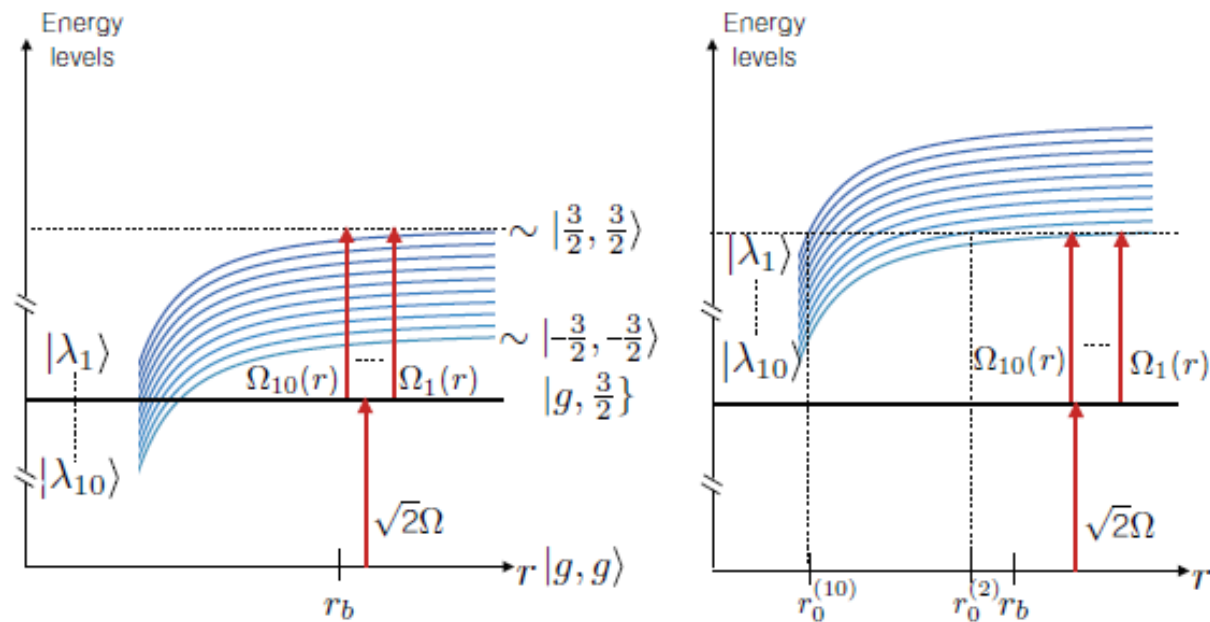


Barredo *et al.*, PRL **112** 183002 (2014)

Vermersch *et al.*, PRA **91** 023411 (2015)

Effect of a B-field

- B-field: Zeeman effect splits $nD_{3/2}, nD_{3/2}$ manifold
- If vdW and Zeeman effect have opposite signs, breakdown of blockade at some ***magic distances***



E-field also matters!

S. Weber *et al.*, [arXiv:1612.08053](https://arxiv.org/abs/1612.08053)

Pair interaction calculator

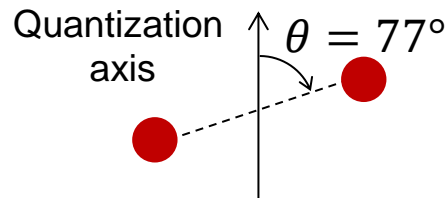
<https://pairinteraction.github.io>



Hans-Peter Büchler

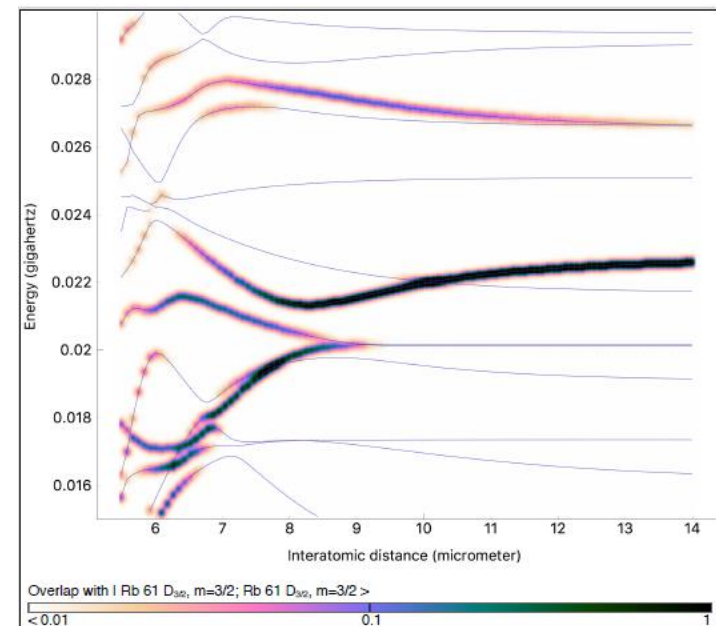
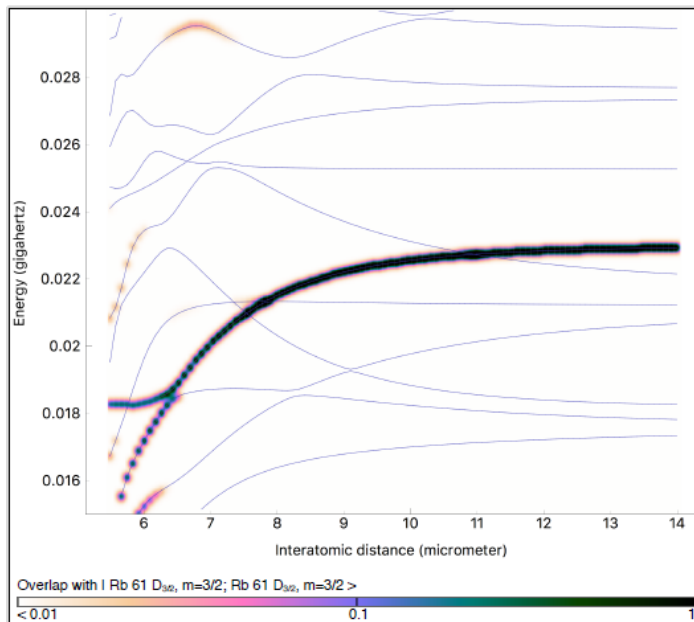


Sebastian Weber

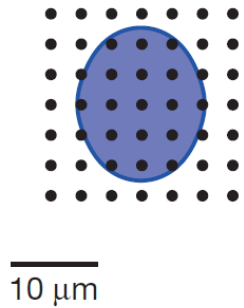


$B = 6.9 \text{ G}$
 $E = 0 \text{ mV/cm}$

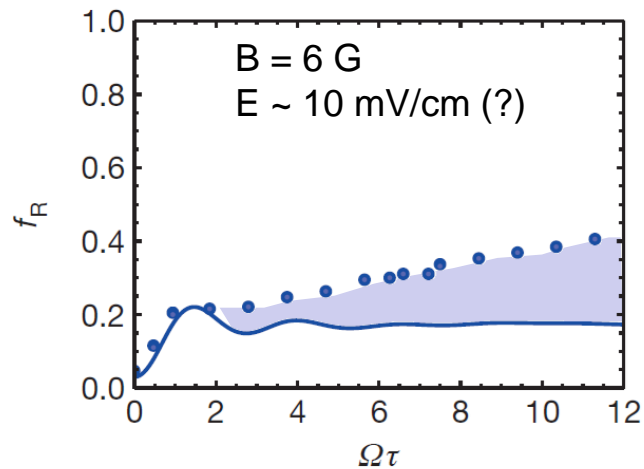
$B = 6.9 \text{ G}$
 $E = 20 \text{ mV/cm}$



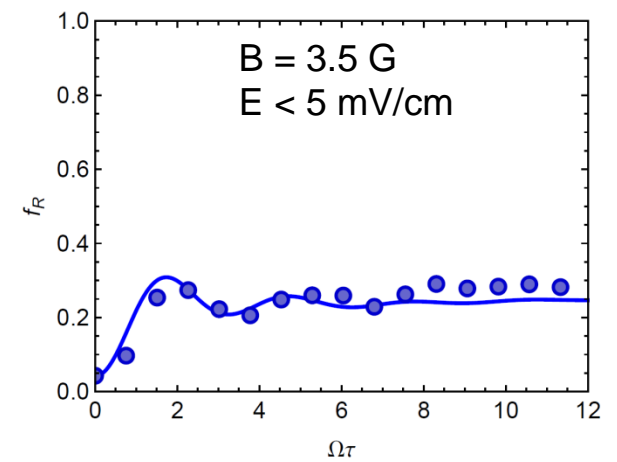
Back to the the 7x7 array...



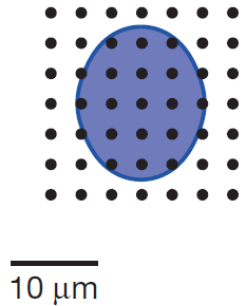
Before...



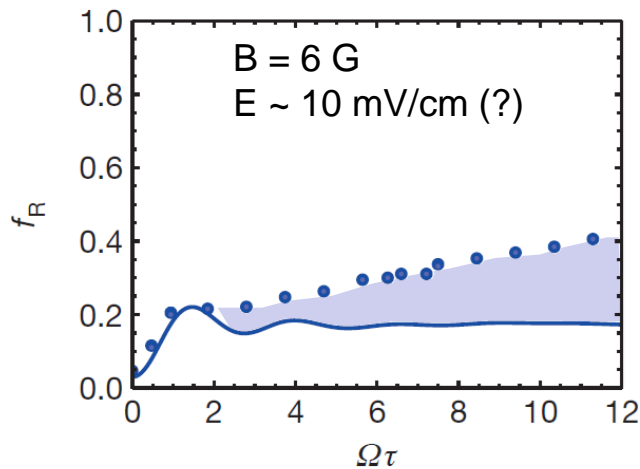
After...



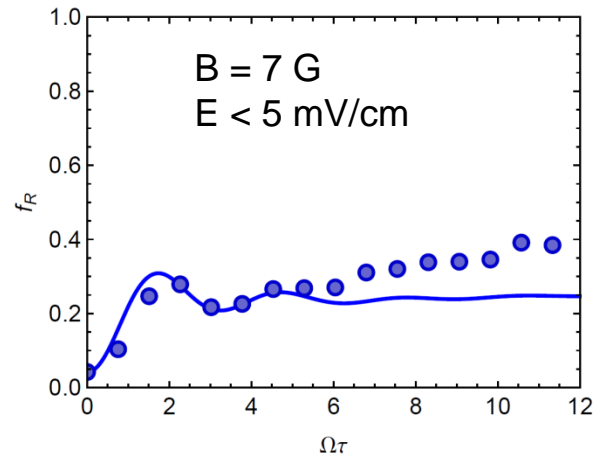
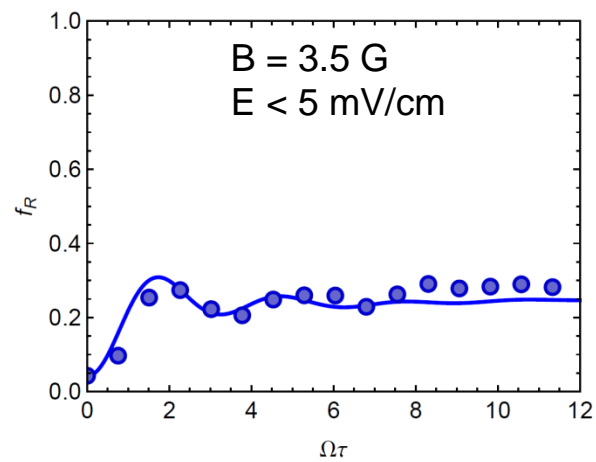
Back to the the 7x7 array...



Before...



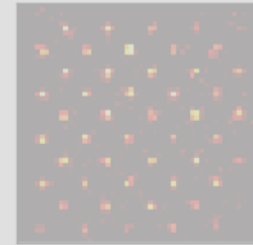
After...



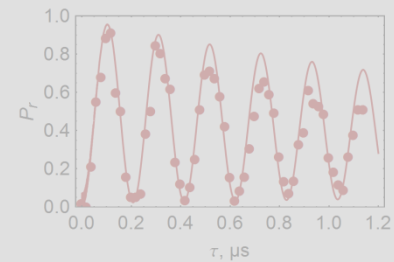
‘Safe’ region in parameter space (E, B, θ) is quite small (especially for high n)

Outline

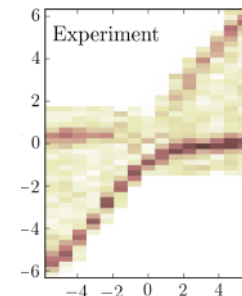
1. Setup and recent results



2. Understanding imperfections



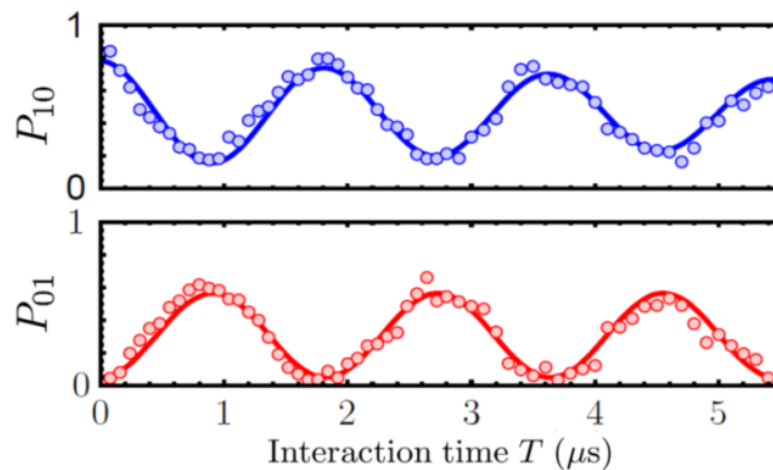
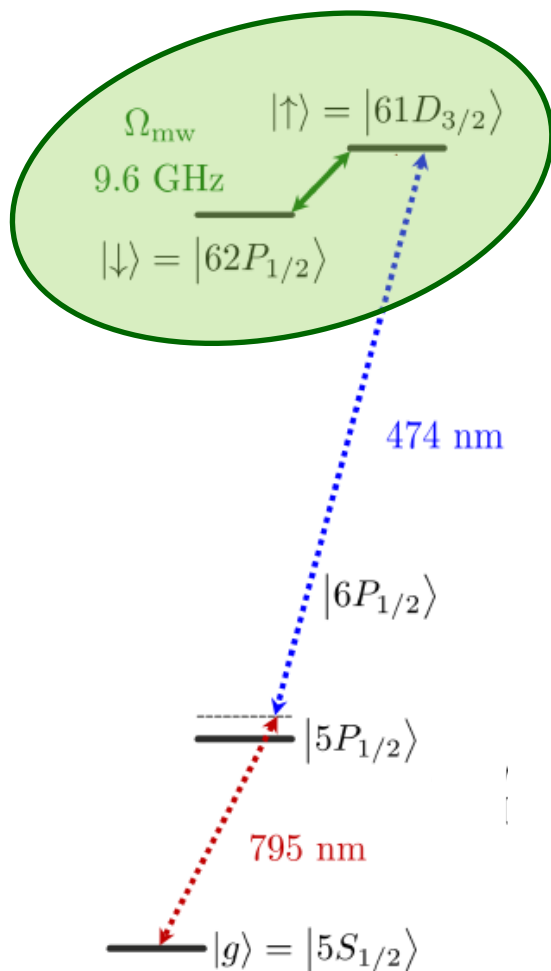
3. Some new tools



Local optical control of XY interactions

Local optical control of the resonant DDI

Resonant dipole-dipole coupling $|\uparrow\downarrow\rangle \leftrightarrow |\downarrow\uparrow\rangle$ **Spin exchange, always “on”**



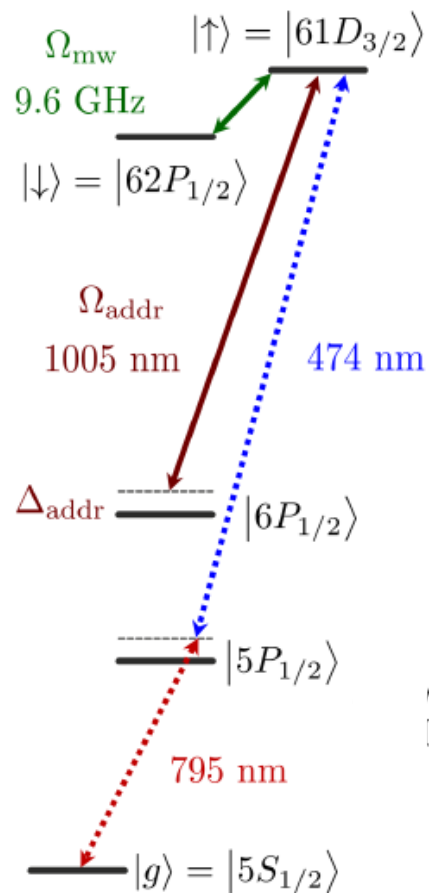
Barredo *et al.*, PRL 2015

How to control this interaction?

Local optical control of the resonant DDI

Resonant dipole-dipole coupling $|\uparrow\downarrow\rangle \leftrightarrow |\downarrow\uparrow\rangle$ **Spin exchange, always “on”**

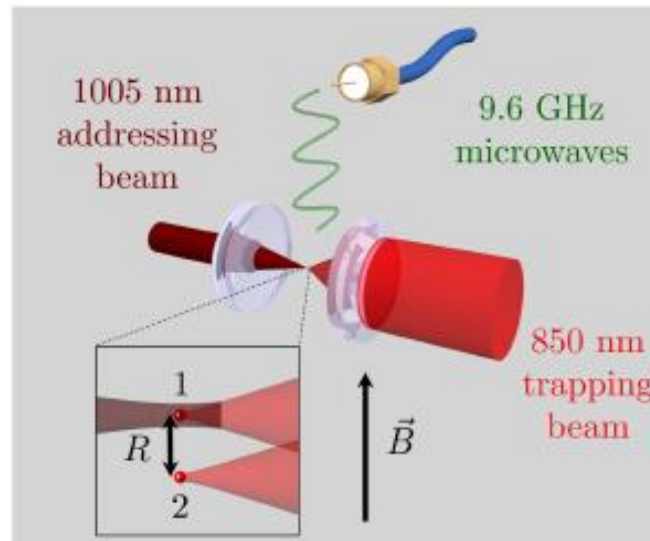
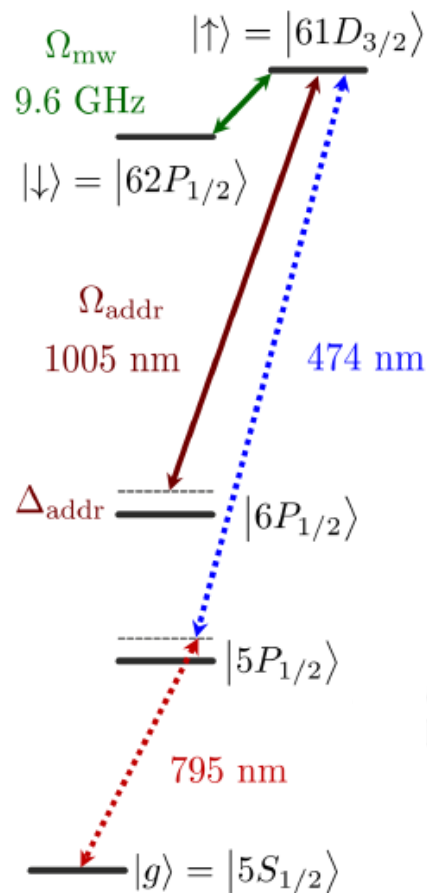
Apply selective lightshift on $|\uparrow\rangle$ with beam at 1005 nm!



Local optical control of the resonant DDI

Resonant dipole-dipole coupling $|\uparrow\downarrow\rangle \leftrightarrow |\downarrow\uparrow\rangle$ **Spin exchange, always “on”**

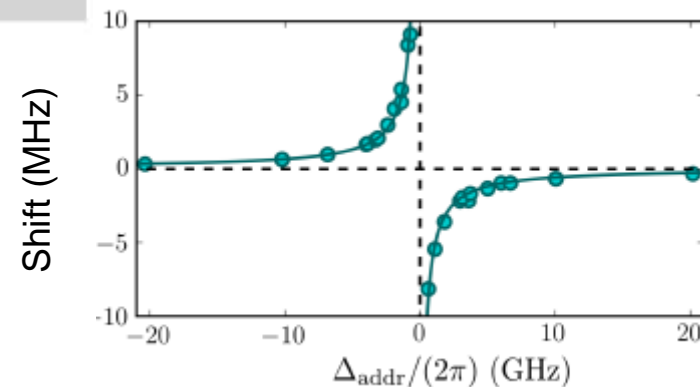
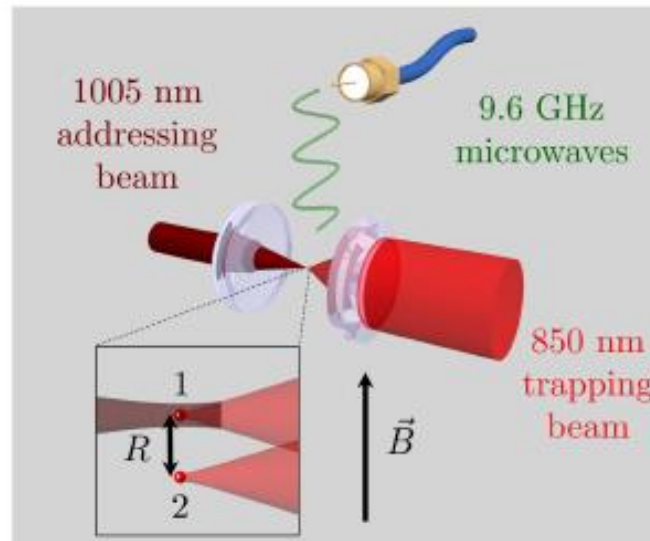
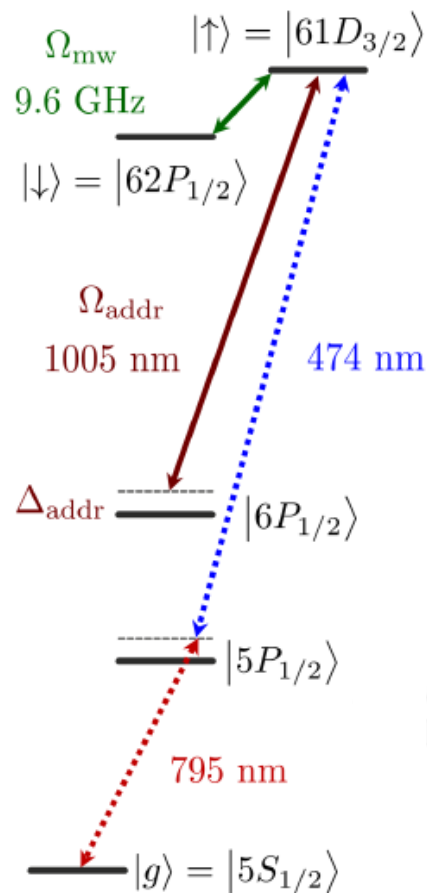
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Local optical control of the resonant DDI

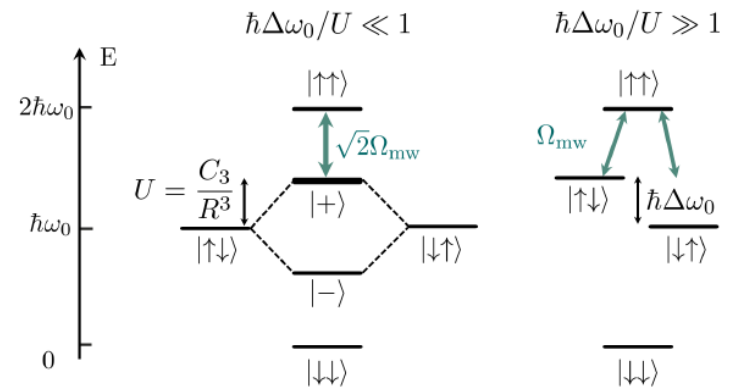
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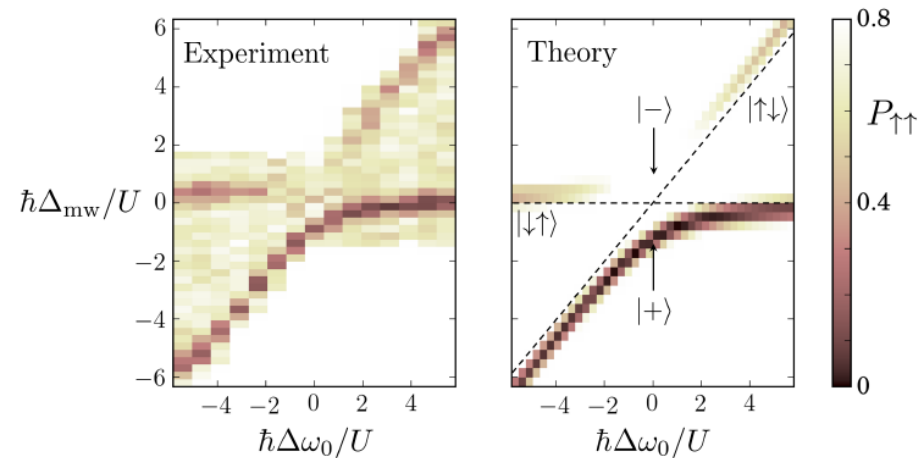


Two atoms

Controlling a two-spin system



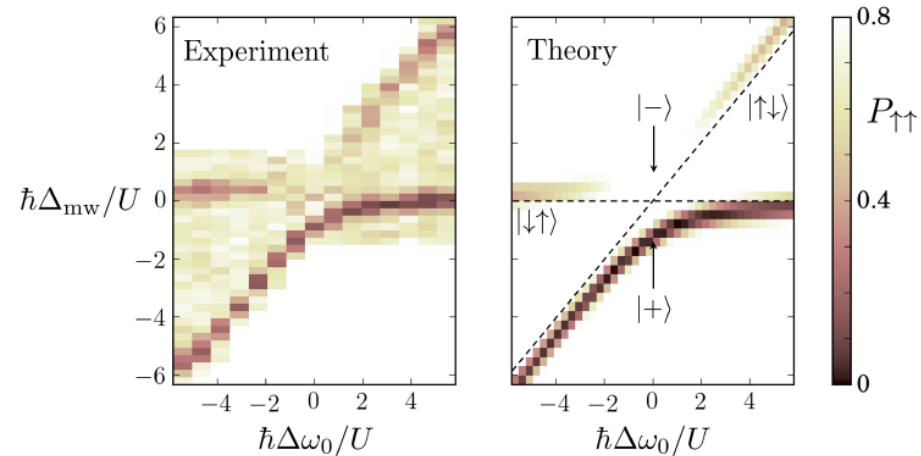
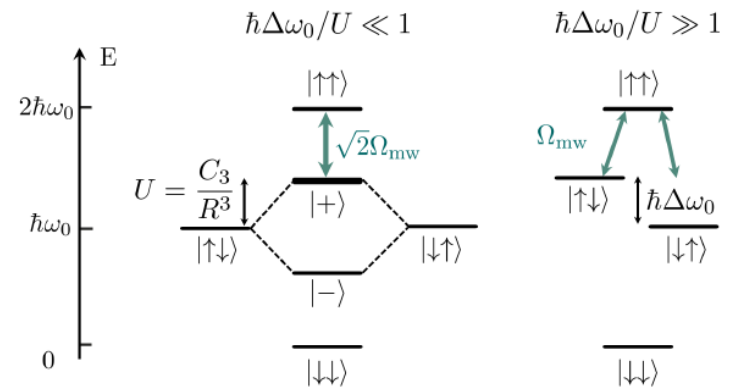
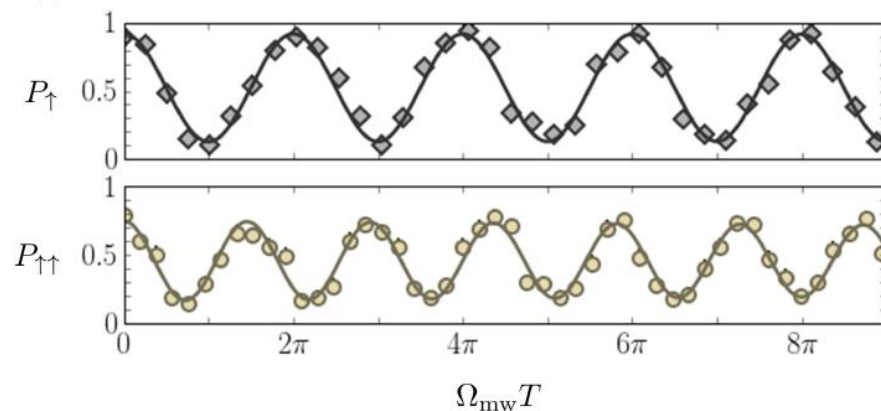
Microwave spectroscopy starting in $|\uparrow\uparrow\rangle$



Two-spin system

Controlling a two-spin system

Microwave spectroscopy starting in $|\uparrow\uparrow\rangle$

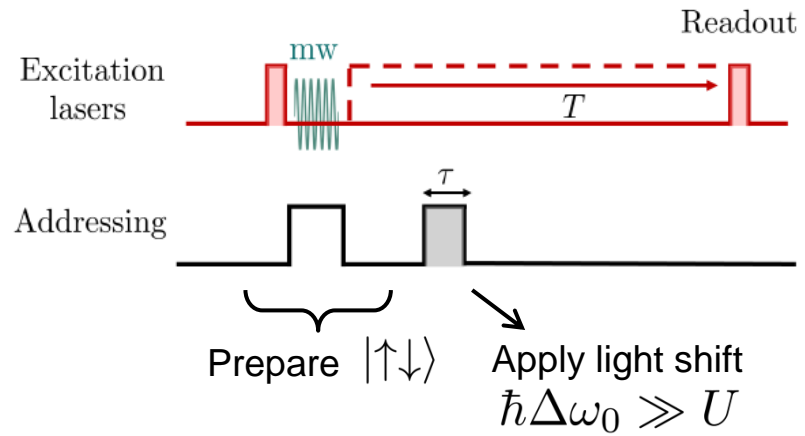
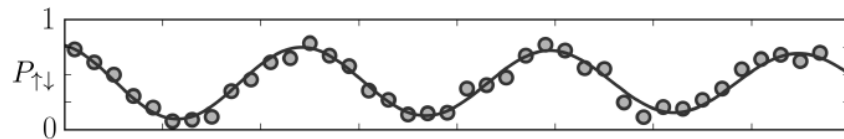


Collective, mw-driven Rabi oscillation between $|\uparrow\uparrow\rangle$ and

$$|+\rangle = \frac{|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle}{\sqrt{2}}$$

Freezing at will the interaction

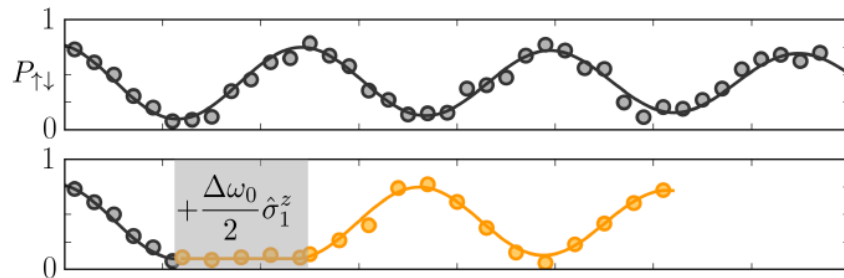
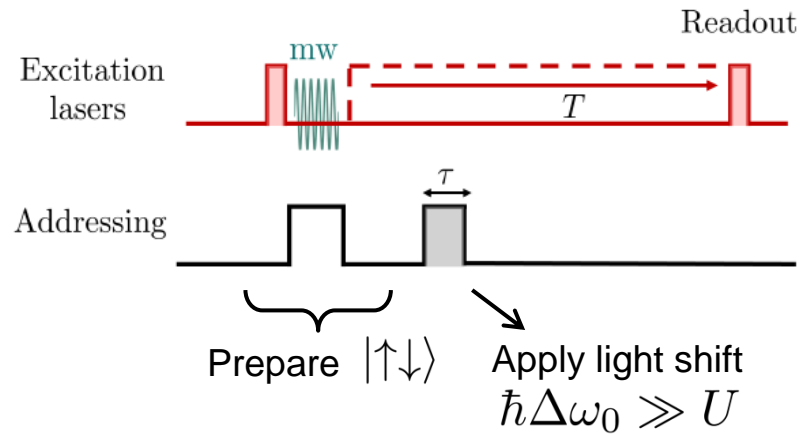
Experimental sequence:



No addressing: regular spin exchange

Freezing at will the interaction

Experimental sequence:

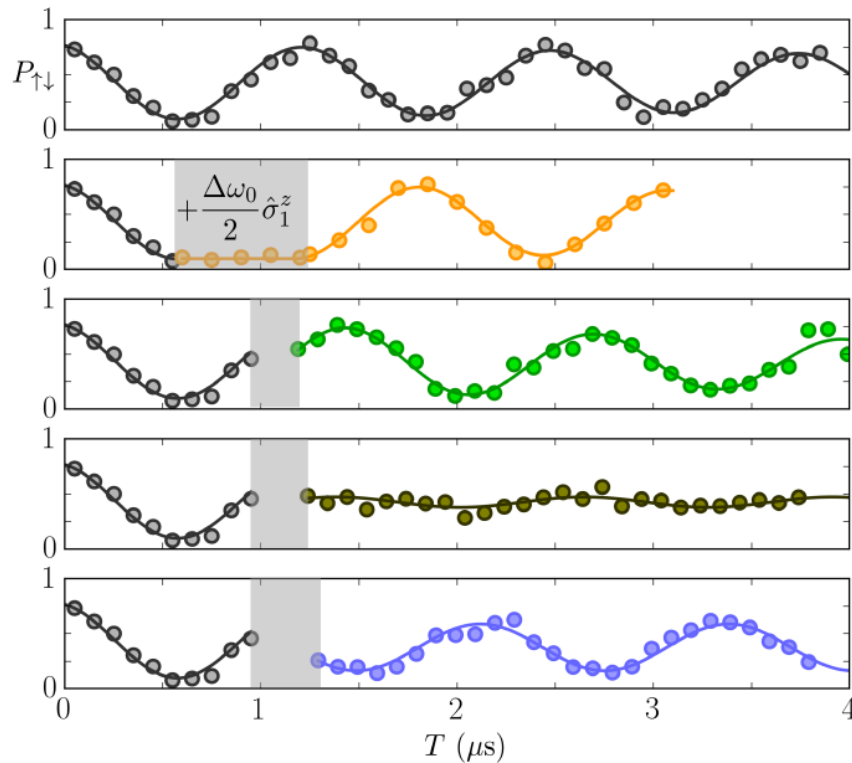
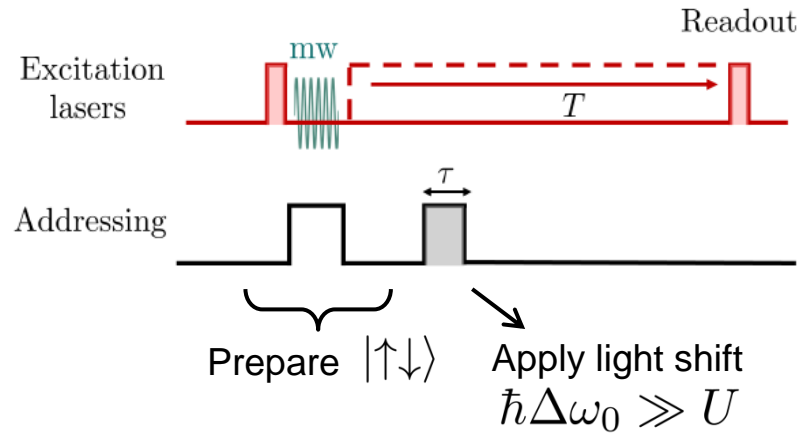


No addressing: regular spin exchange

Freeze dynamics of $|\downarrow\uparrow\rangle$

Freezing at will the interaction

Experimental sequence:



No addressing: regular spin exchange

Freeze dynamics of $|\downarrow\uparrow\rangle$

Freeze a superposition:
influence of the dynamical phase $\Delta\omega_0\tau$

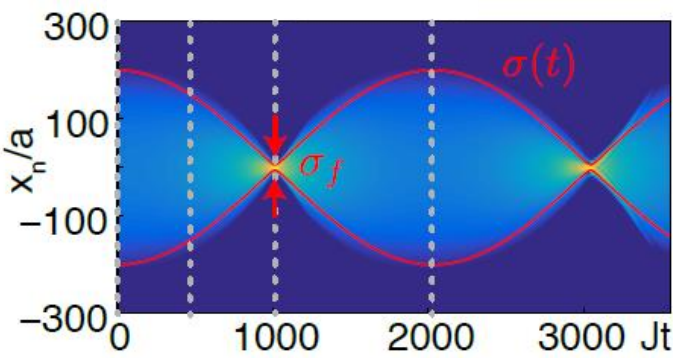
Future applications?

Combining several beams at 1005 nm (e.g. with an SLM)

- ‘Quantum spin lensing’

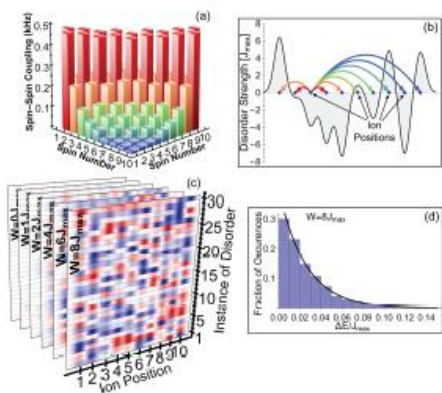
A. W. Glätzle *et al.*, [arXiv:1704.08837](https://arxiv.org/abs/1704.08837)

$$\hat{H} = -J \sum_n \left[\hat{\sigma}_+^{(n)} \hat{\sigma}_-^{(n+1)} + \text{H.c.} \right] + \sum_n V_n \hat{\sigma}_z^{(n)}$$

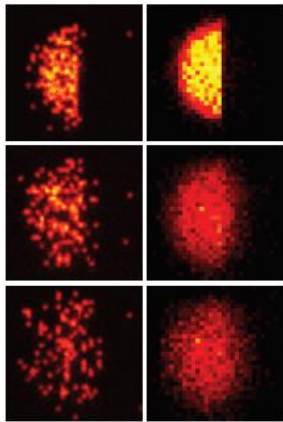


- Controlled disorder: Many-body localization for XY model

Ising 1d (JQI)



Bose-Hubbard 2d (Munich)...



Outlook: Beyond 2D

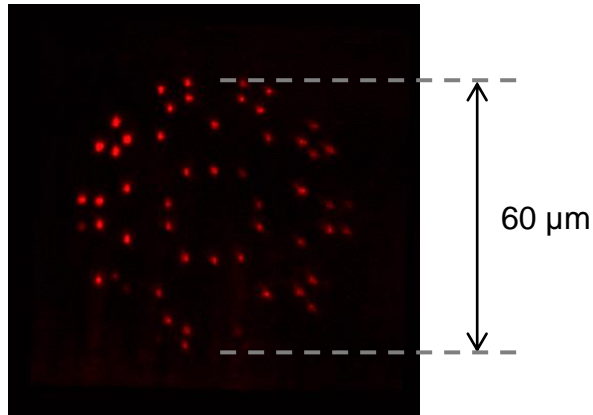
3D holographic arrays

3D arrays of traps

R. Di Leonardo, F. Ianni, and G. Ruocco,
Computer generation of optimal holograms for optical trap arrays,
Optics Express **15**, 1913 (2007)

Work in progress...

Rb₆₀ 'fullerene'



- Long exposure fluorescence imaging (average filling)
- Imaged “slice-by-slice”
- Atom assembler: in progress

Thanks for your attention!